



# A Prioritized Trajectory Planning Algorithm for Connected and Automated Vehicle Mandatory Lane Changes

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# Setting

-Macroscopic routing decision given for each CAV

-Mandatory lane changes (MLCs) guided by routing decisions

-Geometry

-An innermost CAVH dedicated lane with CAVs only

-Other HDV lanes with mixed traffic

-A diverging zone (Zone B) allowing only lane changes of CAVs from dedicated lane into HDV lane

-CAVH intelligence level 3

-Partial Automation

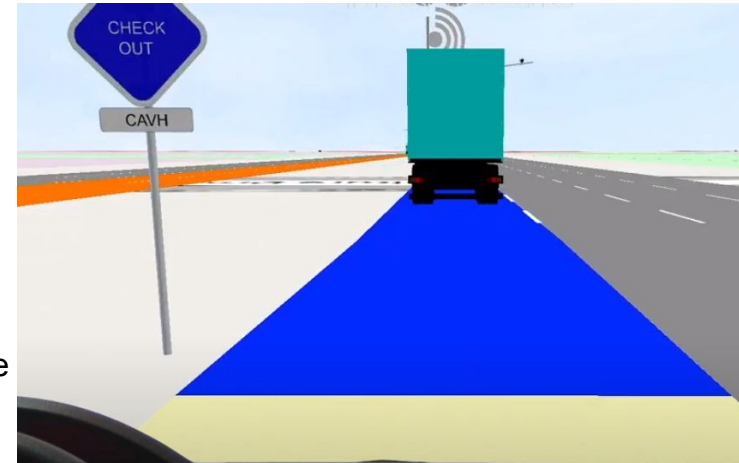
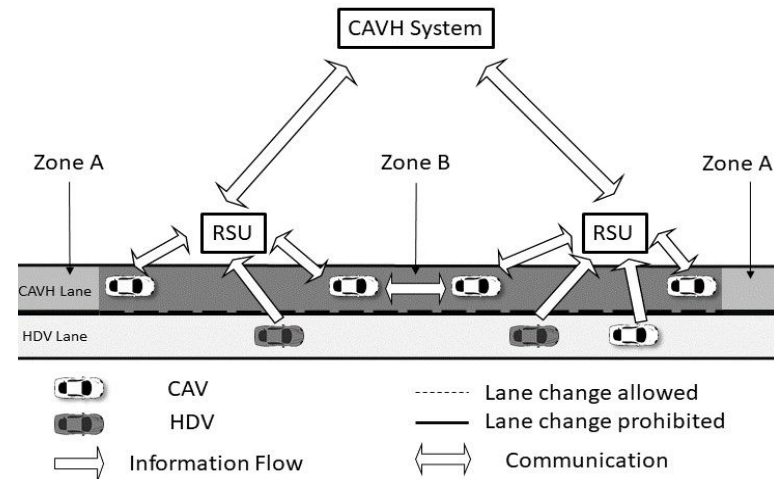
-Driver Assistance System

-Hands off in dedicated lane

-V2V and V2I communication

-Roadside units detect instantaneous information of all vehicles

-System communicates with and controls CAVs in dedicated lane



# Problem Statement



Customers: CAVs executing MLCs from diverging zone into HDV lane

Service: Trajectory Planning, Preparation for MLCs

Our Algorithm

- **Prioritized:** CAVs near the end of the diverging zone given priority in planning
- **System-Optimal:** Minimizes the total travel time for CAVs in the diverging zone for each decision making
- **MLC-Aware:** Gives time and space for consecutive MLCs into the off-ramp
- **Safety-Guaranteed:** Ensures collision avoidance and gap acceptance

# Motivation: MLC



## **Importance:**

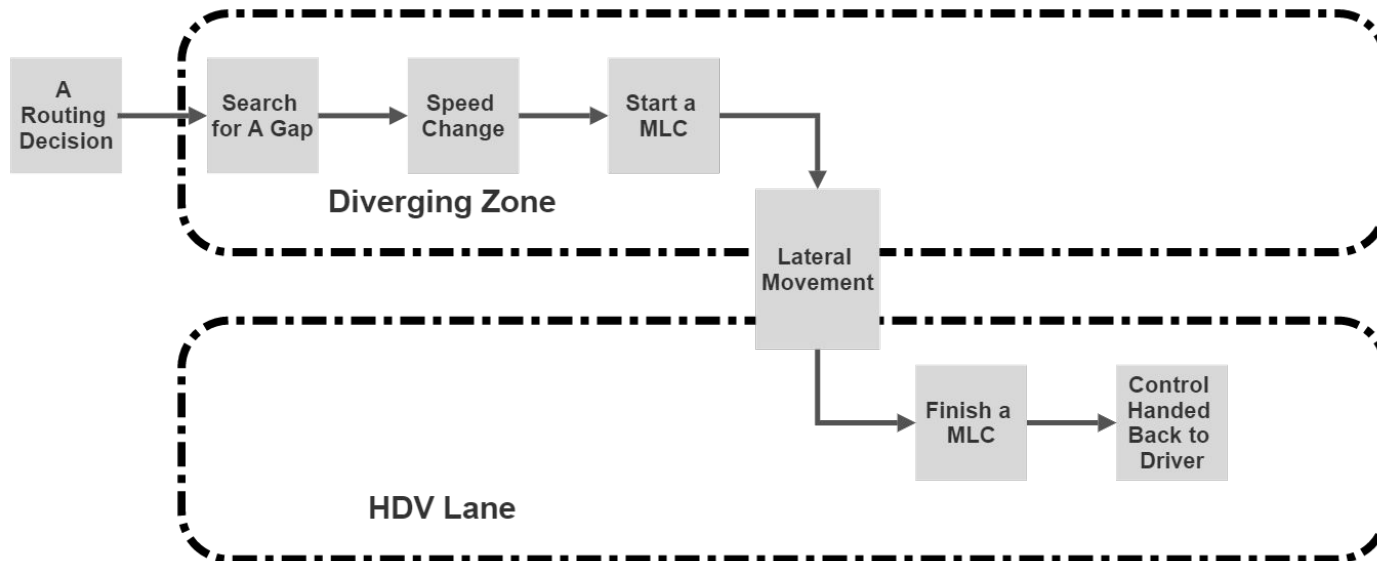
- Guided by routing decisions
- A major reason for congestion at bottlenecks

## **Challenges:**

- Limited length of the the diverging zone
- Urgency posed by routing decision
- Unpredictability of HDVs on the adjacent lane
- Lacks data set
- Few studies considering MLC for CAVs on a system level

# Assumptions

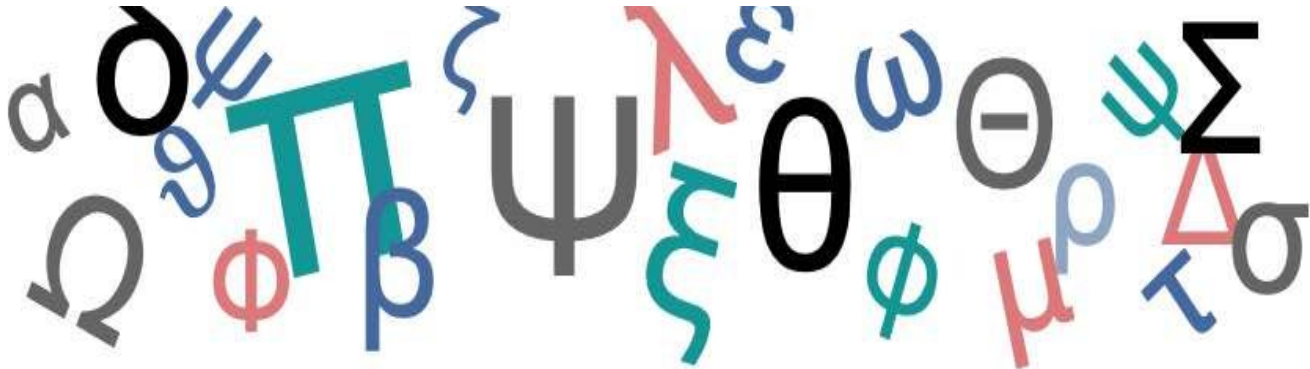
- Passenger cars only in the network
- Offers planning for only processes in the diverging zone



# Definitions: Kinematic Parameter

**Kinematic Parameter:** A parameter chosen by a vehicle that affects its motion

**Sufficient Tuple of Kinematic Parameters:** A tuple of kinematic parameters given which the position is a function of time



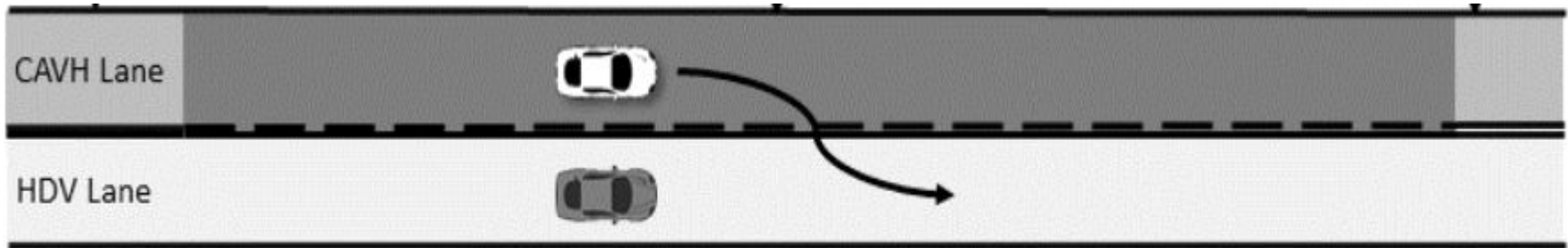
# Definitions: Space Time Slot (STS)

**Space Time Slot (STS):** An ordered pair of time and position

<b>Category\Factors to be satisfied</b>	<b>Central Vehicle Kinematic Parameters</b>	<b>Longitudinal Collision Avoidance</b>	<b>Gap Acceptance on HDV Lane</b>
<b>Reachable STS</b>	Exists at least 1 sufficient tuple	N/A	N/A
<b>Attainable STS</b>	N/A	Satisfied	N/A
<b>Joinable STS</b>	N/A	N/A	Satisfied
<b>Candidate STS</b>	Exists at least 1 sufficient tuple	Satisfied	Satisfied

# Definitions: Trajectory

**Feasible Trajectory:** A trajectory whose STS's are all reachable, attainable under the same sufficient tuple of kinematic parameters, and ends with a candidate STS.





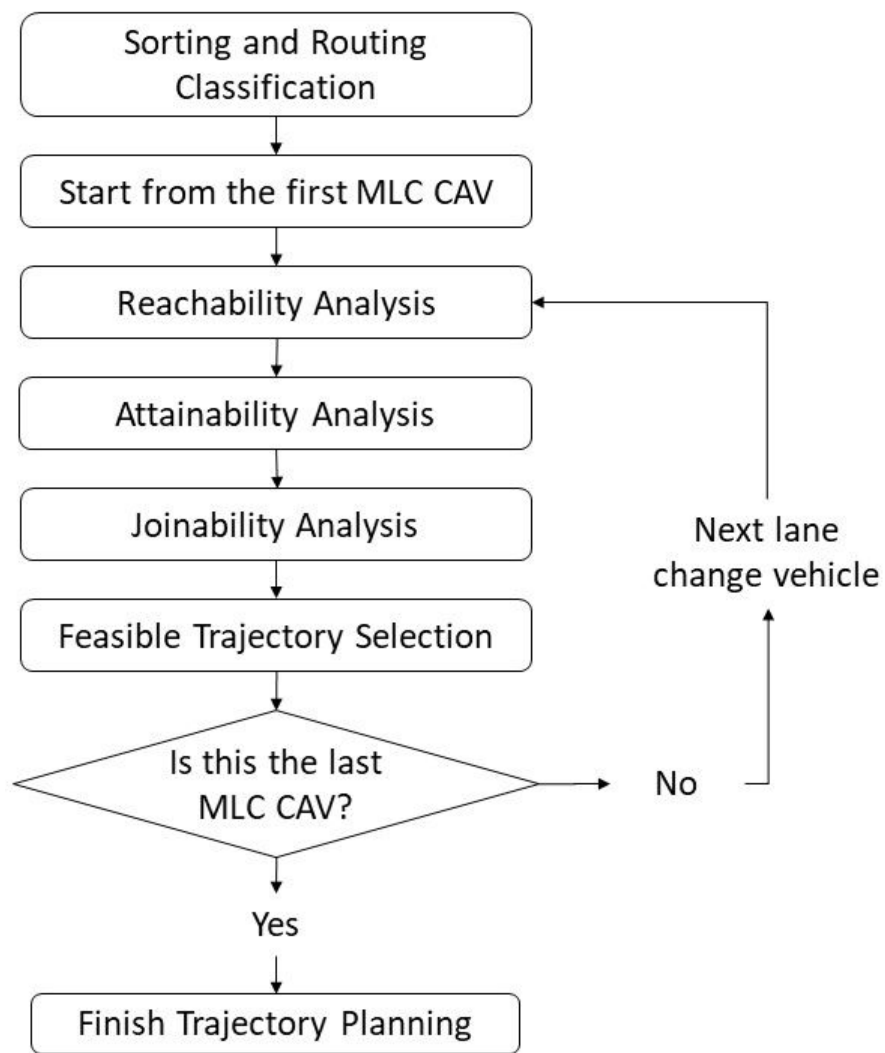
# Algorithm: Framework

## Sorting and routing Classification:

- **Sorting:** Sort the position of CAVs in the diverging zone with descending order
- **Classification:** Classify the routing decisions of CAVs
- **Extract HDVs:** Based on HDVs' location, extract those that could influence MLC CAVs' decisions
- **Predict HDVs:** Predict or Interpolate the future positions of HDVs

## Start iteration:

- Start iterating over each MLC CAV in the diverging zone



# Algorithm: Framework

## Reachability Analysis:

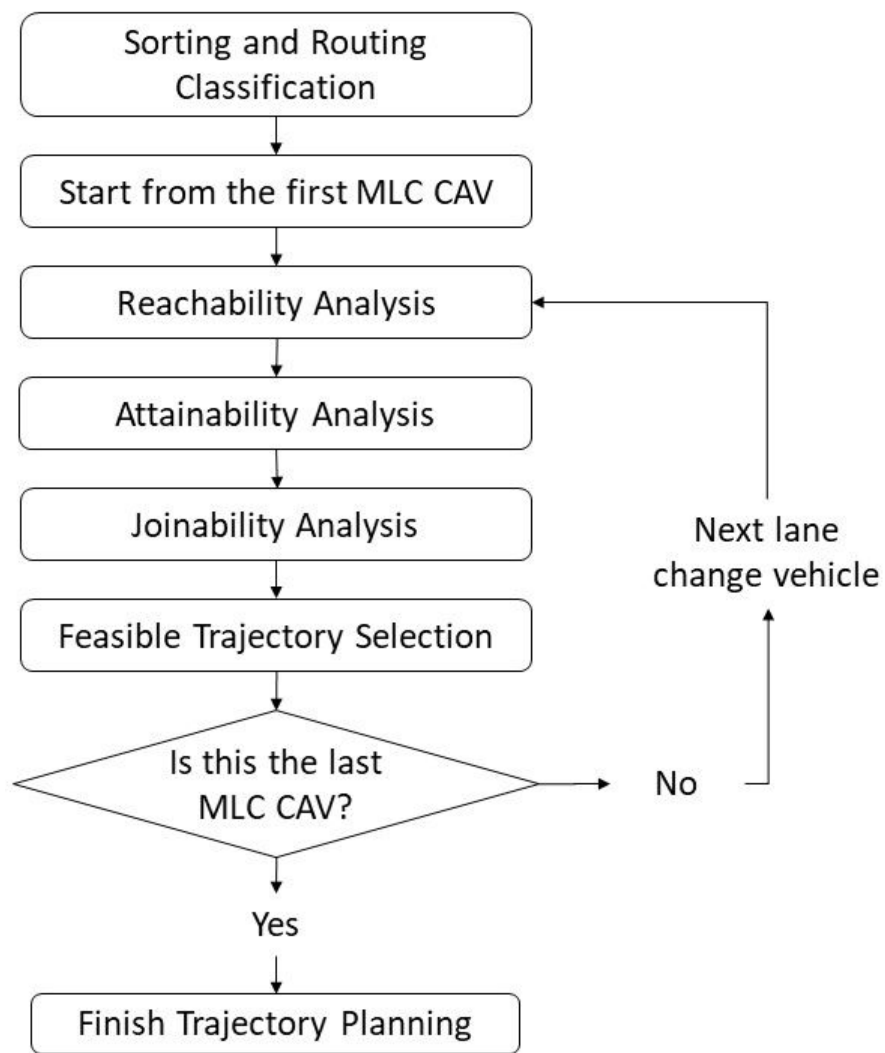
- Get all possible sufficient tuples of kinematic parameters
- Get all reachable STS's of a MLC CAV
- Organize reachable STS's by kinematic parameters

## Attainability Analysis:

- Get all attainable STS's based on leading MLC CAVs' optimal trajectory, leaving space for non-MLC CAVs

## Joinability Analysis:

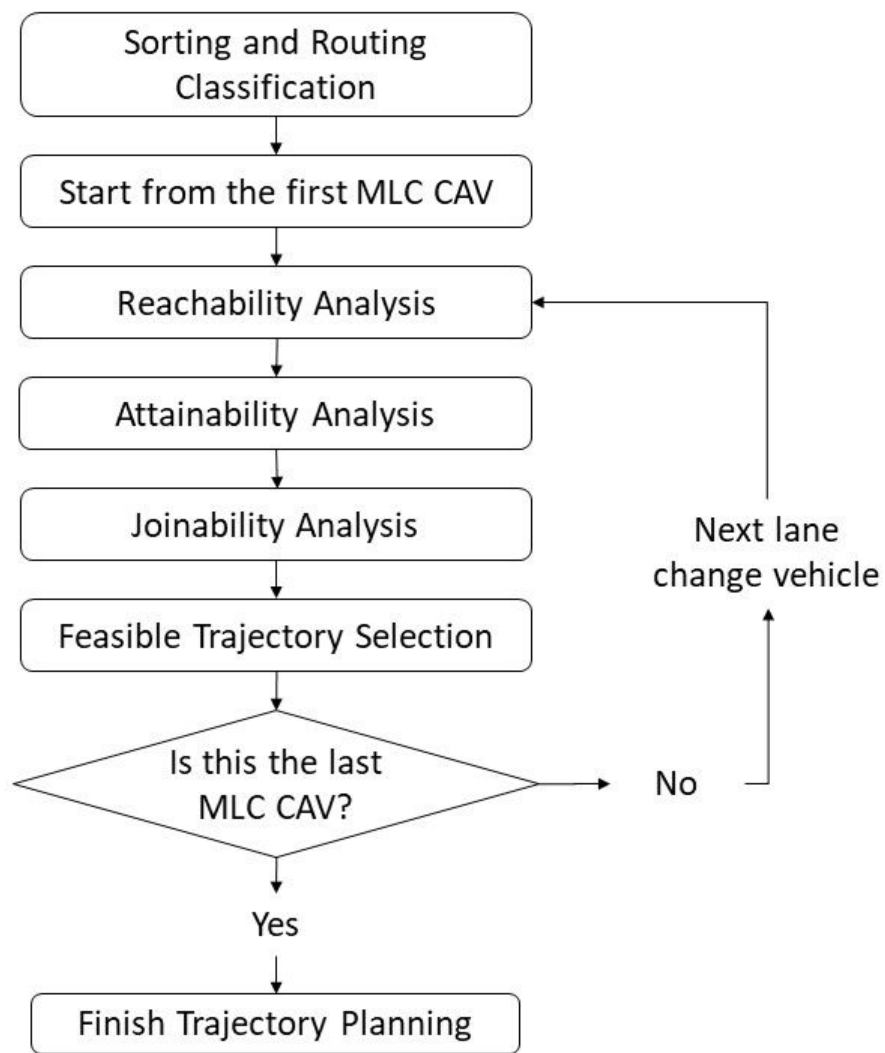
- Based on the interpolated trajectories in HDV lane, get all joinable STS's



# Algorithm: Framework

## Feasible Trajectory Selection:

- Get all candidate STS's by taking the intersection of reachable, attainable and joinable STS's
- Extract feasible trajectories that ends at each candidate STS's
- Among the feasible trajectories, select the optimal trajectory based on a cost function
- Interpolate the motion in the HDV lane after the CAV's MLC, and reserve the spacing

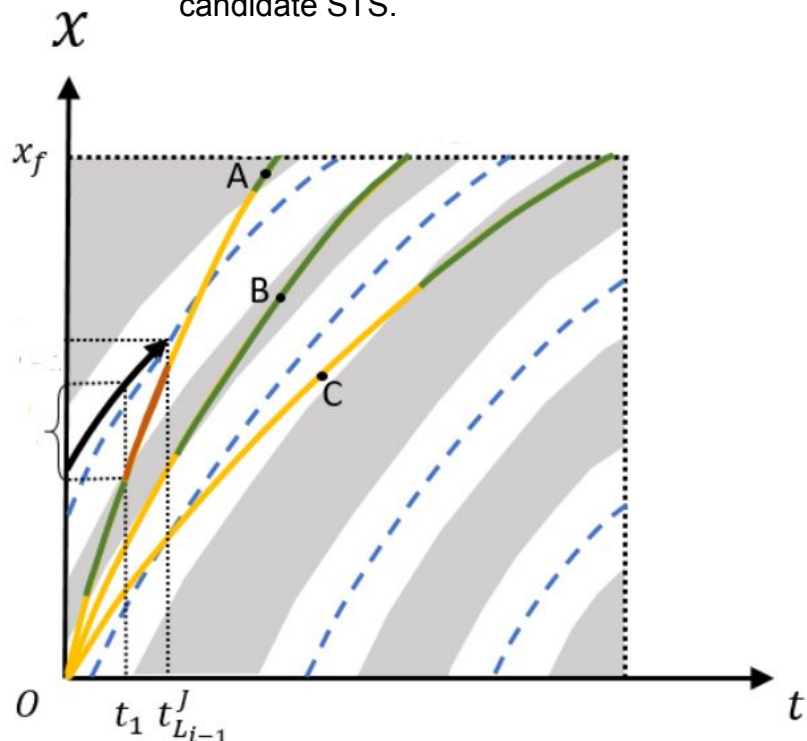


# Algorithm: Framework

Example:

- 3 sufficient tuples of kinematic parameters available
- **Dashed Line:** HDV trajectories
- **Black Arrow:** Leading CAV in the Diverging Zone
- **Shaded Area:** Joinable STS's
- **Red Line:** Reachable, but not Attainable
- **Yellow Line:** Reachable, Attainable but not Joinable
- **Green Line:** Candidate STS's
- **OB:** A Feasible Trajectory

Feasible Trajectory: A trajectory whose STS's are all reachable, attainable under the same sufficient tuple of kinematic parameters, and ends with a candidate STS.



# Case Study



## **Car Following Model:** Spring Mass Damper Model with no Leader

- Only 1 element in each sufficient tuple of kinematic parameter

## **Cost Function:**

- 1) Total delay in the diverging zone
- +
- 2) Expected detour time if a CAV fails to exit at the target off-ramp

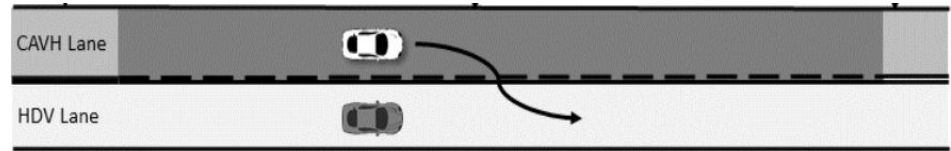
## **HDV Speed Prediction Model:** Uniform Speed Prediction

- Advantage: Do not need to perform training
- Disadvantage: Lacks Accuracy

# Simulation

## Geometry:

- An inner CAVH dedicated lane
- An outer HDV lane
- 1500m of diverging zone



## Initialization:

- 5 CAVs with initial speed of 100km/h and position randomized in the first 500m of diverging zone
- 8 HDVs with initial speed between 60km/h and 100km/h, desired speed between 80km/h and 100km/h, and random initial position in the HDV lane
- Vehicles in HDV lane use Newell car-following model

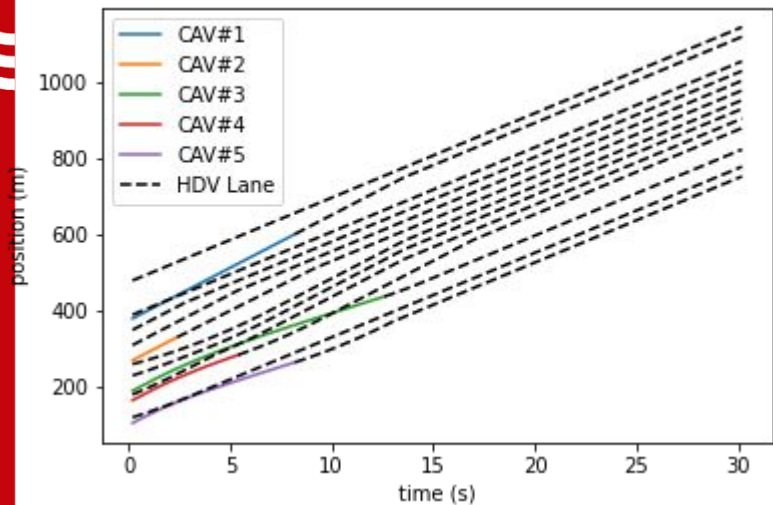
## Comparison:

- Prioritized System-Optimal Algorithm **vs.** Gap Acceptance Model

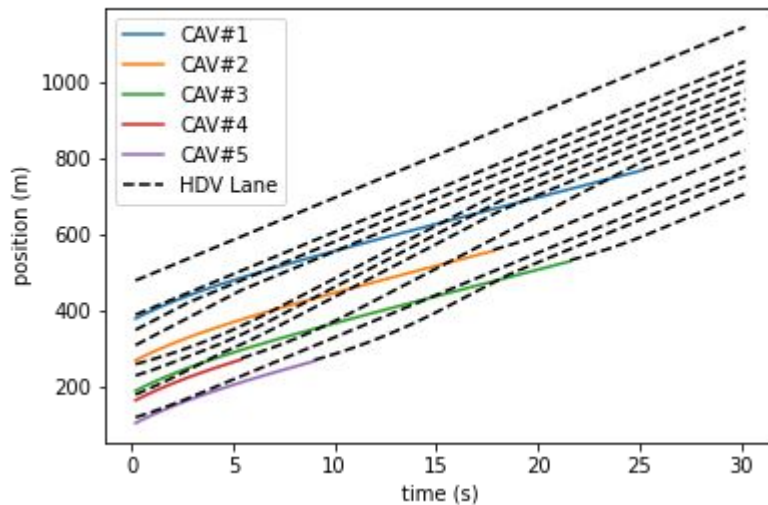
# Results: Position-Time Diagram



Prioritized System-Optimal Algorithm

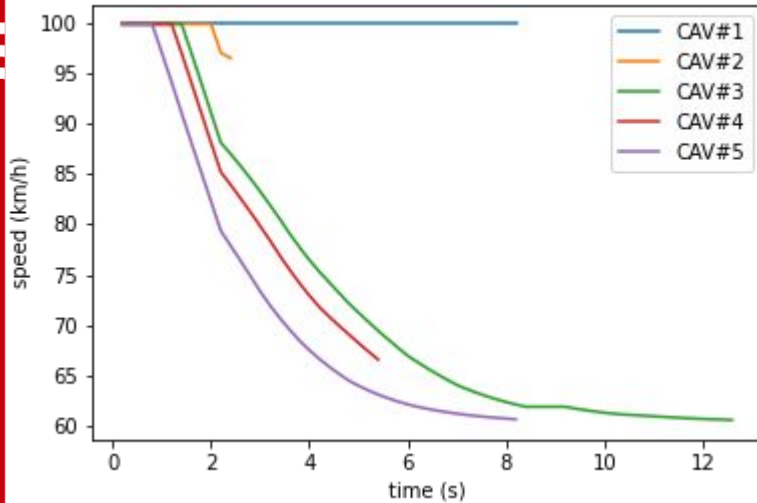


Gap Acceptance Model (Theoretical)

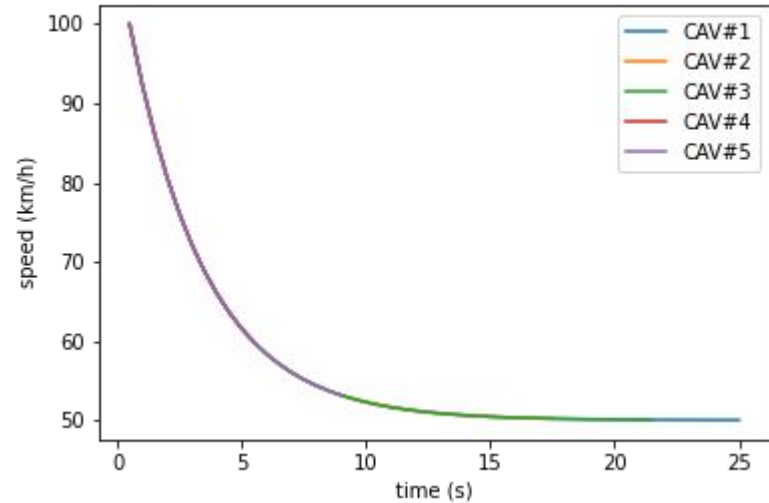


# Results: Speed-Time Diagram (Diverging Zone)

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Prioritized System-Optimal Algorithm



Gap Acceptance Model (Theoretical)





# Results: Metrics

<b>Metric/Model</b>	<b>Gap Acceptance Model</b>	<b>Prioritized System- Optimal Algorithm</b>
<b>Average Speed in Diverging Zone</b>	63km/h	85km/h
<b>Average Distance Driven before a MLC</b>	257.82m	162.1m
<b>Average Time Driven before a MLC</b>	15.60s	7.16s
<b>Calculation Time per CAV</b>	N/A	0.03s

# Results: Discussions



## Advantages of Prioritized System-Optimal Algorithm:

- Produced relatively smooth speed change
- Earlier time taken before MLC executions
- Earlier distance driven before MLC executions
- Higher average speed in the diverging zone
- Efficient utilization of spacing in HDV lane
- Relatively low run-time

# Future Research



## Sources of Improvements:

- Examine the application of other car-following models
- Test on other cost functions
- Apply machine learning to forecast trajectories in the HDV lane
- Carry out a larger-scaled simulation to further examine the efficiency
- Consider semi-trucks and buses in the algorithm



# Thanks for Listening!

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